

Kinetics of Solubilization of Oils that are **Soluble** or **Insoluble** in Pure Water: Comparison of Theory and Experiment

Peter A. Kralchevsky, N. D. Denkov, N. C. Christov,
P. D. Todorov, **G. Broze**, **P. Durbut** and **A. Mehreteab**

Laboratory of Chemical Physics & Engineering
Faculty of Chemistry, University of Sofia, BULGARIA

Colgate-Palmolive R&D, Inc., Milmort (Herstal), Belgium

**Colgate-Palmolive Technology Center, Piscataway, New
Jersey, USA**

PLAN

1. Mechanisms of solubilization: bulk and surface reaction;
2. Used experimental methods;
3. Solubilization of decane and benzene in solutions of **SDS**;
4. **Triglycerides**: **ionic** surfactants – inhibitors of solubilization;
5. **Triglycerides**: trb. copolymers – promoters of solubilization;

Two Major Mechanisms of Solubilization

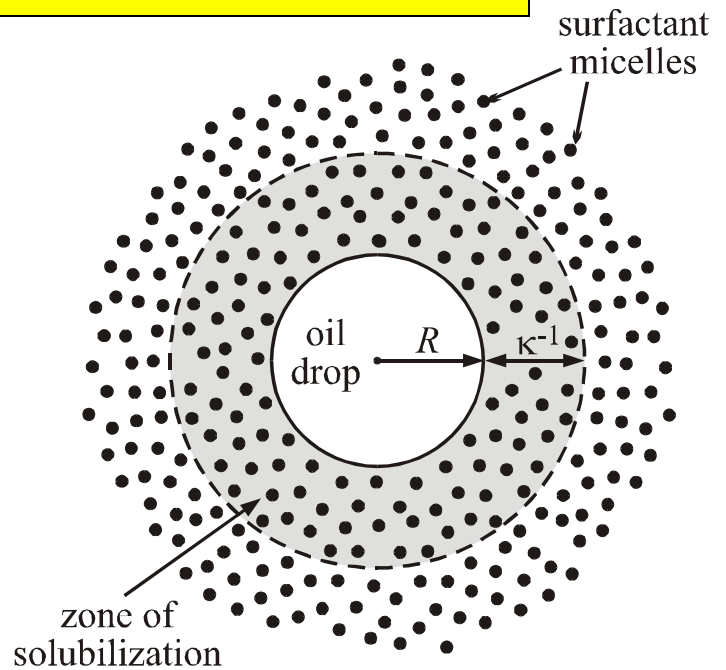
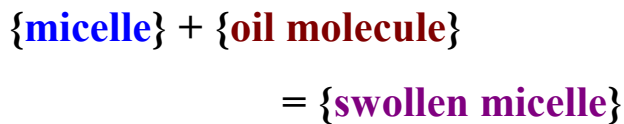
(A) Bulk Reaction:

- the oil is soluble in pure water
- **micelles capture oil molecules**

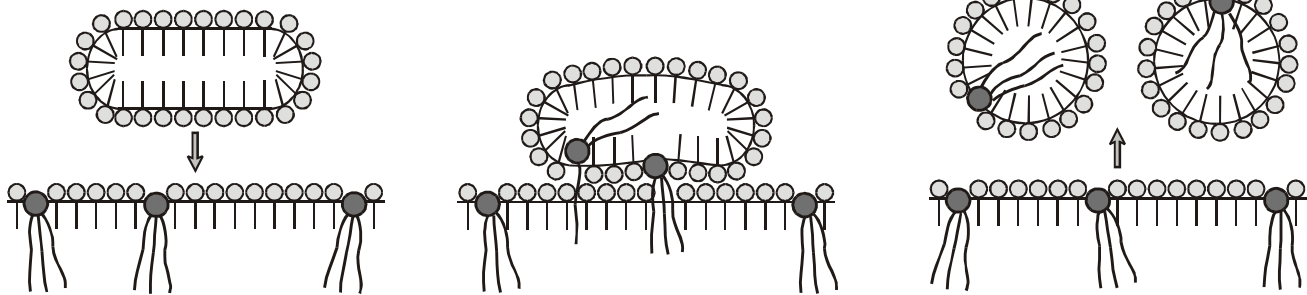
Kinetic parameters:

α – mass transfer coefficient

k_+ – rate constant of the reaction



(B) Surface Reaction:



(a) Micelle adsorption

(b) Uptake of oil

(c) Desorption

- the oil is insoluble in pure water (like the **triglycerides**)

- parameters of the model:

k_a – rate constant of adsorption (Stage 1)

k_s – rate constant of the surface reaction (Stage 2)

k_d – rate constant of desorption (Stage 3)

Aim of the study: to determine the kinetic parameters

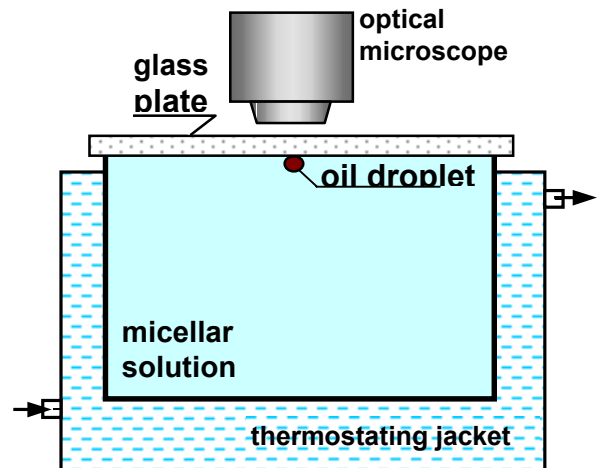
Experimental Methods

1. Simple Solubilization Cell (Cell # 1)

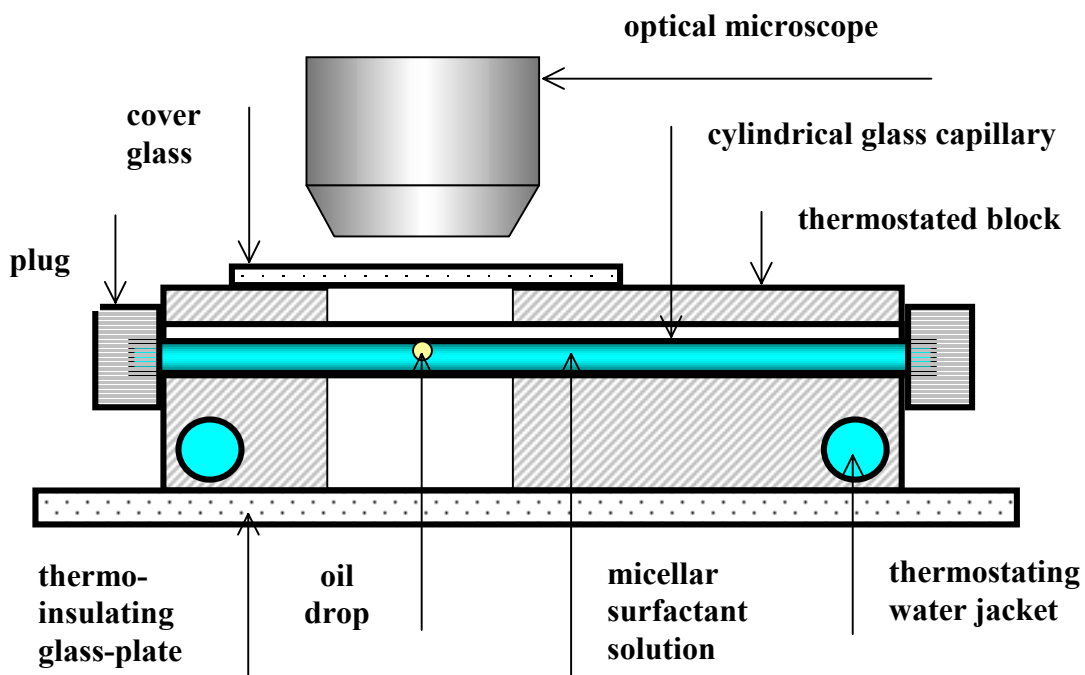
(2 × 2 × 1.5 cm)

Advantage: Easy to operate

Disadvantage: the kinetics is influenced by uncontrollable thermal convections



2. Capillary Cell (Cell # 2)



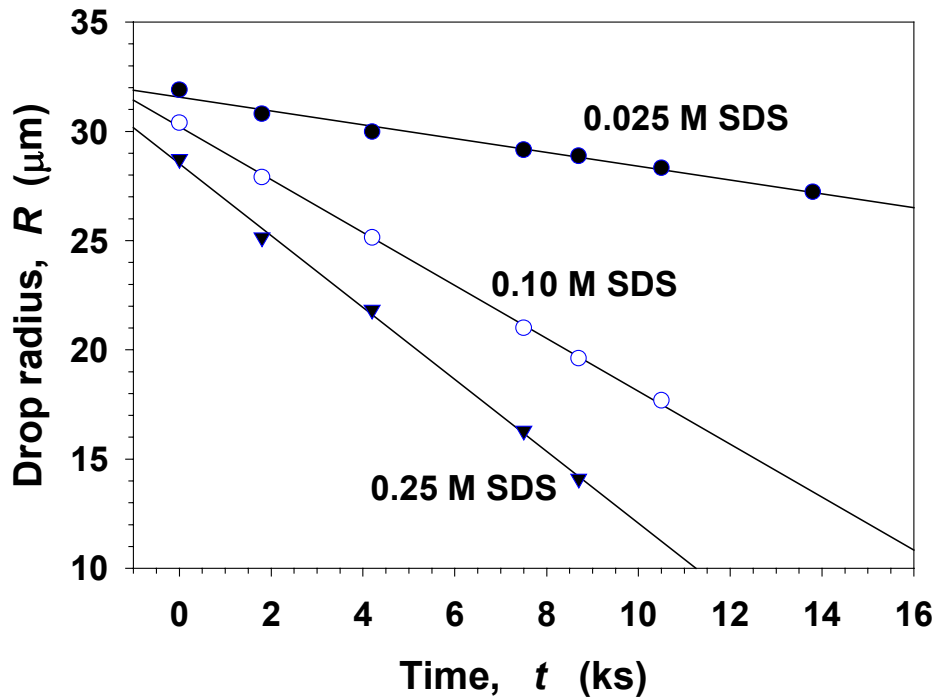
- horizontal capillary of inner diameter $2R = 0.06 \text{ cm}$ ($= 600 \mu\text{m}$);
- a single oil drop is injected by syringe;
- the solubilization occurs under a purely diffusion regime (no thermal convections) \Rightarrow quantitative interpretation is possible.

n-Decane and Benzene in Water Solutions of SDS

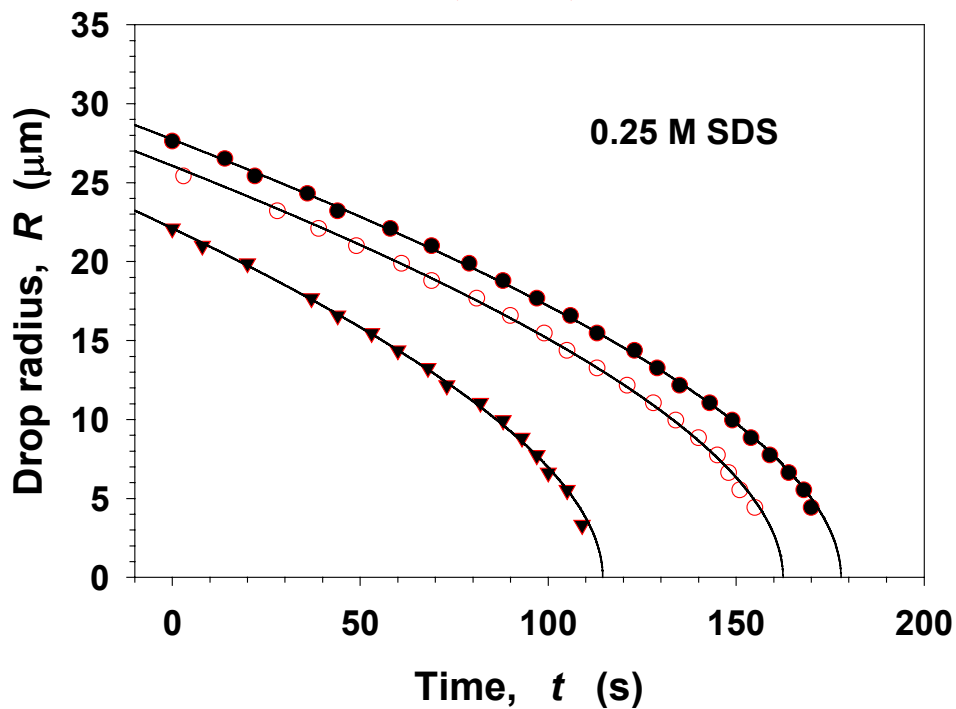
[P. D. Todorov et al. *J. Colloid Interface Sci.* 245 (2002) 371–382]

Dependence of the solubilization rate on the SDS concentration

Decane; SDS; 27°C



Benzene; SDS; 27°C



Theoretical Model

Stationary Diffusion

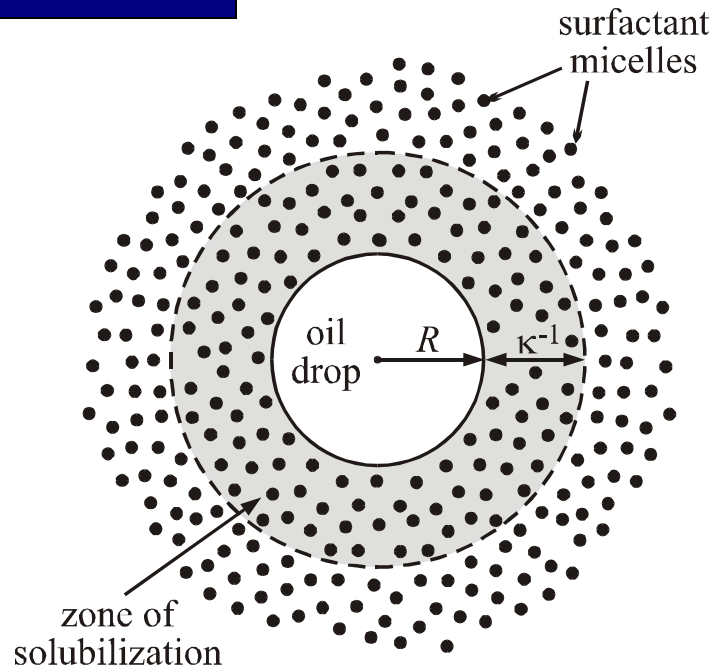
+ Reaction of Solubilization:

$$D_{\text{oil}} \nabla^2 c_{\text{oil}} = k_+ c_{\text{tot}} c_{\text{oil}}$$

Boundary Condition:

$$-\left. \frac{\partial c_{\text{oil}}}{\partial r} \right|_{r=R} = \alpha [c_{\text{eq}} - c_{\text{oil}}(R)]$$

α – mass transfer coefficient



$$c_{\text{oil}}(r) = \frac{c_{\text{eq}} R}{1 + (\kappa + R^{-1})/\alpha} \frac{\exp[\kappa(R-r)]}{r}$$

$$\kappa^2 = k_+ c_{\text{tot}} / D_{\text{oil}}$$

Solubilization Flux:

$$Q_{\text{oil}} = -D_{\text{oil}} \left. \frac{\partial c_{\text{oil}}}{\partial r} \right|_{r=R}$$

Diminishing of the Drop Volume:

$$-\frac{dV}{dt} = v_{\text{oil}} (4\pi R^2) \lambda Q_{\text{oil}}$$

V_{oil} – volume per oil molecule;

Wall:
$$\lambda \approx \frac{0.9 + 4.725 \kappa R + 2.1 (\kappa R)^2}{1 + 5.25 \kappa R + 2.1 (\kappa R)^2}$$

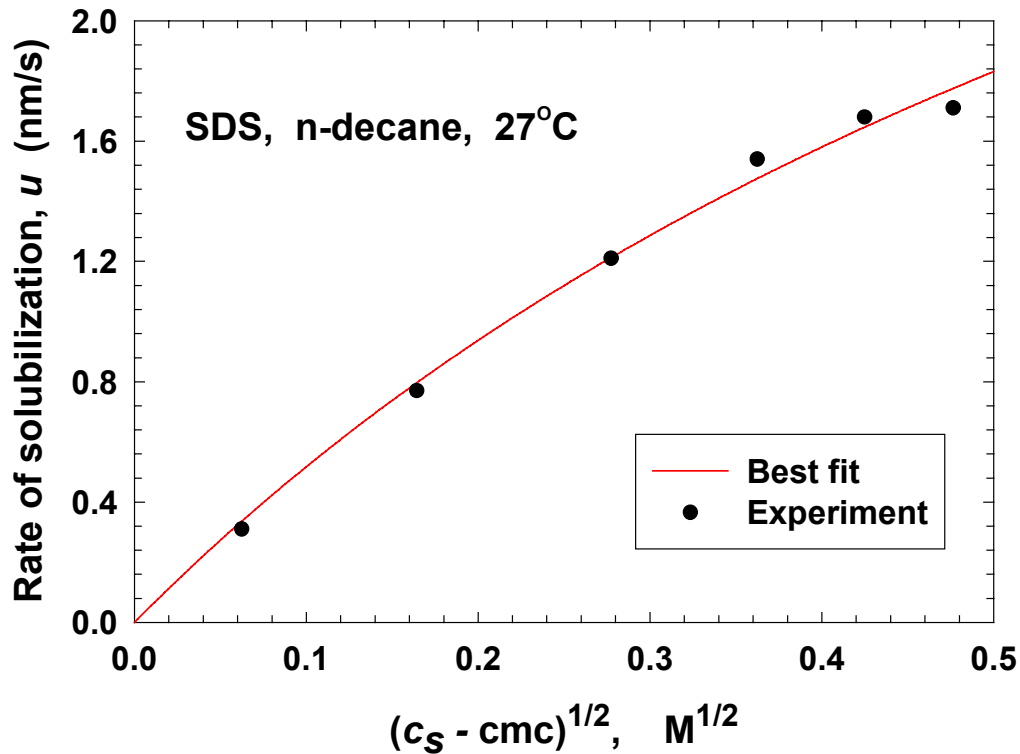
$$\frac{dR}{dt} = -\frac{\alpha \beta (1 + \kappa R)}{1 + (\alpha + \kappa) R} \lambda(\kappa R),$$

$$\beta = v_{\text{oil}} D_{\text{oil}} c_{\text{eq}}$$

Results for n-Decane

In the limit $\kappa R \gg 1 \Rightarrow -\frac{dR}{dt} \approx \text{const.} \equiv u = \frac{a(c_s - \text{cmc})^{1/2}}{b + (c_s - \text{cmc})^{1/2}}$

(narrow solubilization zone)



From the fit we determine:

$$\alpha = 29.8 \pm 5.8 \text{ } (\mu\text{m}^{-1})$$

(mass transfer coefficient)

$$k_+ = (1.02 \pm 0.34) \times 10^{-13} \text{ } (\text{cm}^3/\text{s})$$

(rate constant: oil uptake by micelles)

SDS concentration	Solubilization rate	Width of solubilization
c_s (M)	u (nm/s)	zone: κ^{-1} (nm)
0.025	0.31	267
0.25	1.71	61

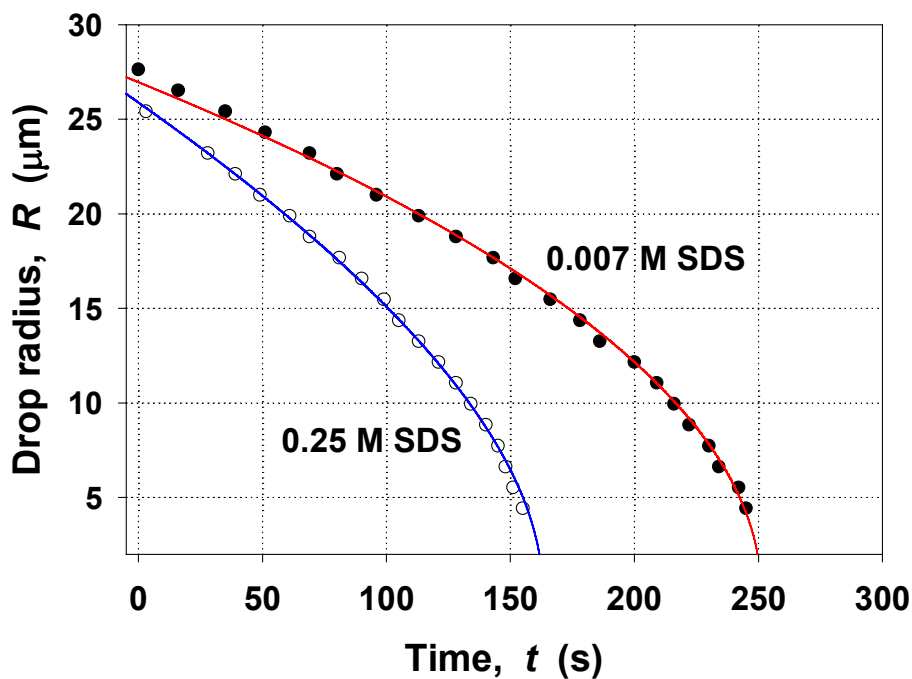
Results for Benzene

Fast dissolution of benzene in water $\Rightarrow \alpha \rightarrow \infty, \quad c_{\text{oil}}|_{r=R} = c_{\text{eq}}$

$$\Rightarrow \frac{dR}{dt} = -\frac{\beta}{R}(1 + \kappa R)\lambda(\kappa R)$$

(1) Purely molecular dissolution of oil: **no micellar solubilization**, $\kappa = 0$)

$$R(t) = \sqrt{1.8 \beta(t_0 - t)}, \quad R(t_0) = 0 \quad \text{(No adjustable parameters!)}$$



(2) Simultaneous **molecular dissolution** and **micellar solubilization**:

κ – adjustable parameter;

$$k_+ = \kappa^2 D_{\text{oil}} / c_{\text{tot}}$$

Benzene: $k_+ = 2.3 \times 10^{-19} \text{ (cm}^3/\text{s)}$, $\kappa^{-1} = 40.1 \text{ } \mu\text{m}$, **(0.25 M SDS)**

n-Decane: $k_+ = 1.0 \times 10^{-13} \text{ (cm}^3/\text{s)}$

Under diffusional control: $k_+ = 4\pi D_{\text{oil}} r_{\text{mic}} \approx 2.4 \times 10^{-11} \text{ (cm}^3/\text{s)}$

\Rightarrow **Barrier control** of the uptake of **oil molecules** by the **micelles**

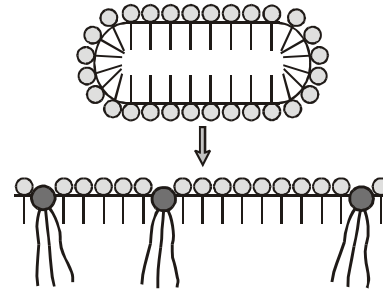
Insoluble Oils: Surface Reaction

Triglyceride solubilization by **nonionic surfactant** $C_{12}EO_n$ ($n = 5$ or 6)

A necessary step:

Micelle adsorption

at **oil/water** interface

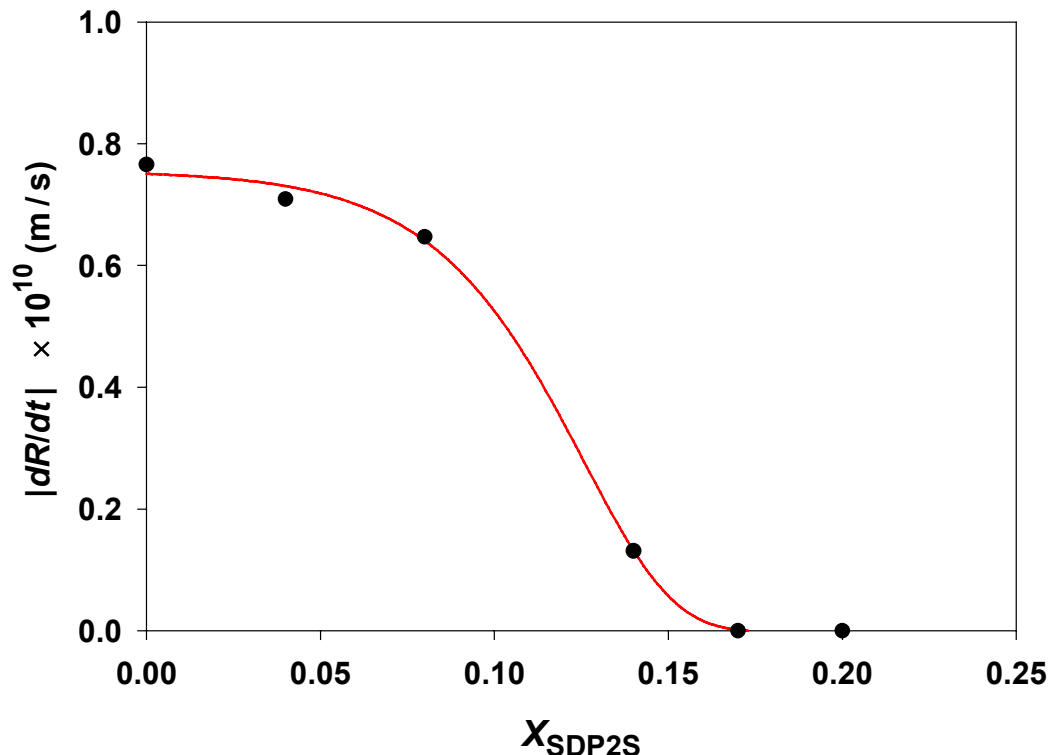


oil phase

KEY: Repulsion due to the surface electric charge suppresses the micelle adsorption and the solubilization.

EXAMPLE: (Added **ionic** surfactant **inhibits** the solubilization)

12 mM $C_{12}E_6$ (**nonionic**) + SDP2S (**ionic**) + 0.2 M Na_2SO_4



$$X_{SDP2S} = C_{SDP2S} / (C_{C12EO6} + C_{SDP2S})$$

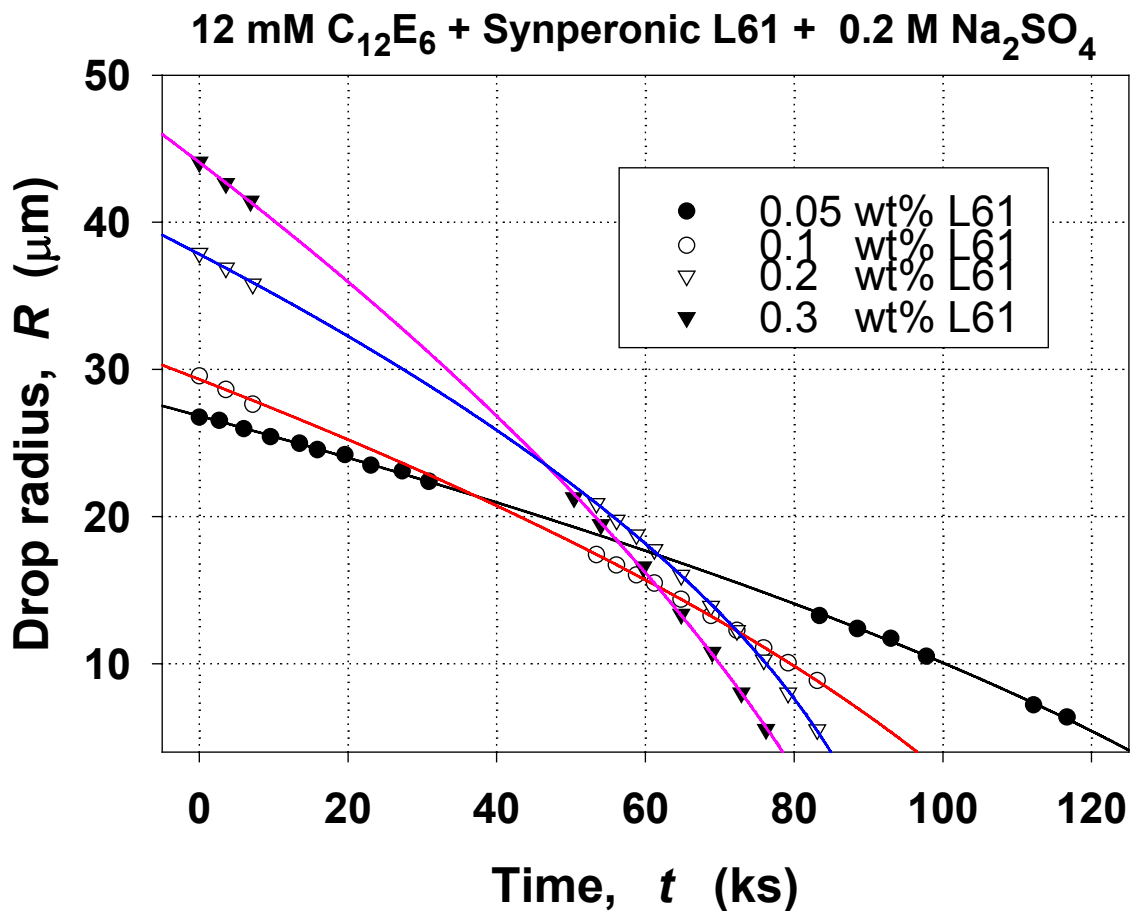
EO_n-PO_m-EO_n Triblock Copolymers as Promoters of Solubilization

Materials:

C₁₂H₂₅(C₂H₄O)₅, [C₁₂E₅] + 0.01 M NaCl

C₁₂H₂₅(C₂H₄O)₆, [C₁₂E₆] + 0.2 M Na₂SO₄

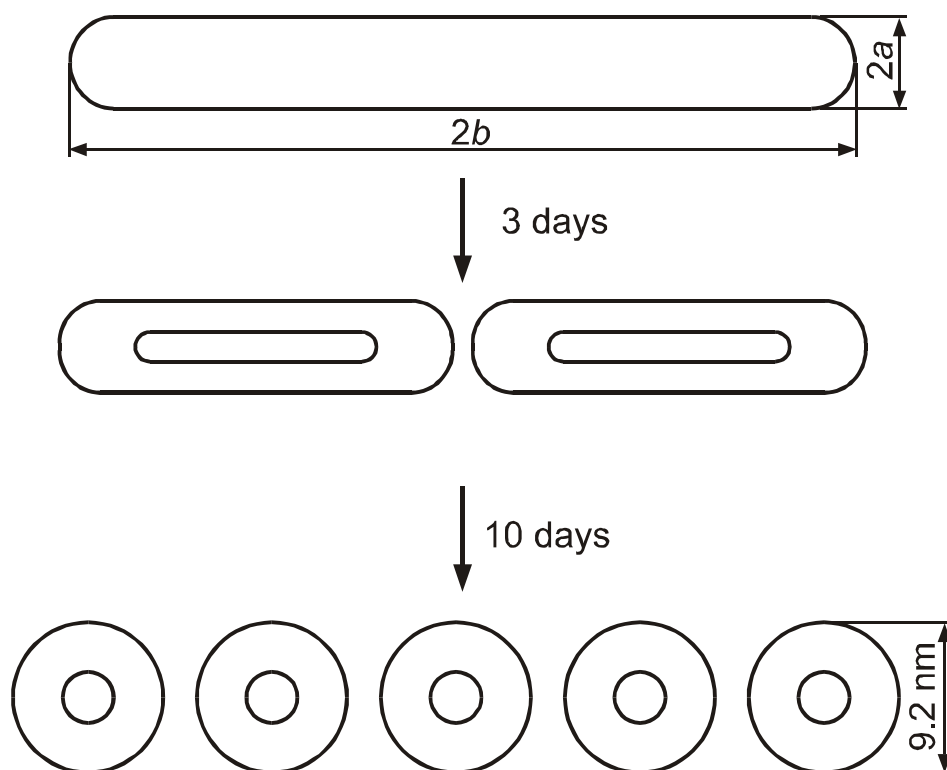
Synperonic L61: [EO_{2.5}PO₃₄EO_{2.5}] (molecular weight: 2100)

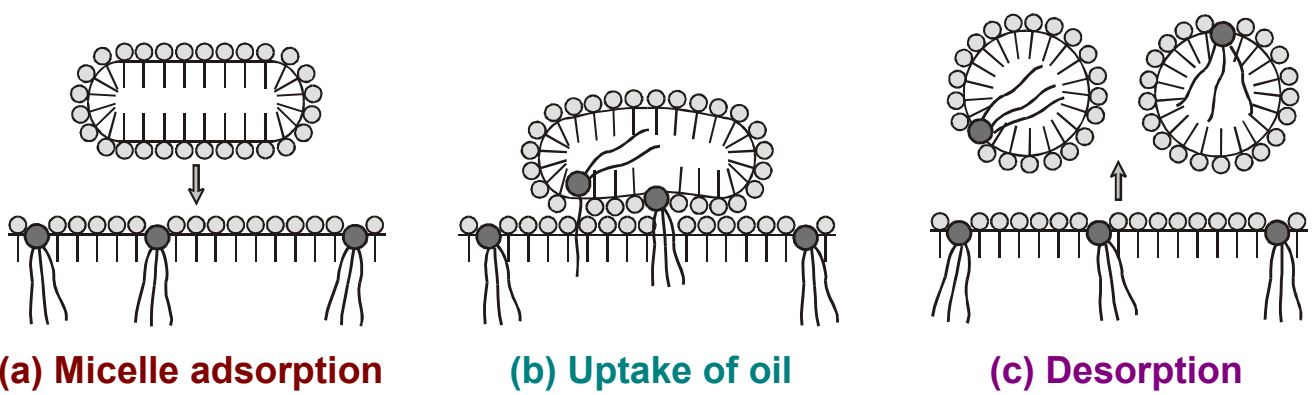


Mixed Micelles of $C_{12}E_5$ + Synperonic L61

SL61 (wt%)	$N_{\text{surfact.}}$	N_{SL61}	N_{triolein}	eccentricity p	a (nm)
Empty Micelles					
0.1	1841	77	0	24	2.8
0.2	895	74	0	21	2.4
0.3	726	90	0	17	2.5
10 days contact with oil					
0.1	341	13	20	1	4.6
0.2	261	22	15	1.3	4.1
0.3	235	29	12	3.3	3.0

12 mM $C_{12}E_5$ + 0.1 wt % SL61 + 0.01 M NaCl





Equation provided by the model for diminishing of the drop radius R :

$$R(t) = \alpha \{ [1 + 2\beta(t_0 - t)]^{1/2} - 1 \} / \beta$$

$$(\alpha, \beta) \rightarrow (\chi, n_s); \quad \chi = k_s k_a / (k_s + k_d) \approx k_a \quad (k_s \gg k_d);$$

C_{SL61} (wt %)	rate constant χ ($\mu\text{m/s}$) [drop]	oil molecules per swollen micelle n_s [drop]	oil molecules per swollen micelle n_s [NMR]
Solutions of 0.012 M $C_{12}EO_5$ + 0.01 M NaCl			
0.0	0.20	—	—
0.1	0.34	20	20 ± 3
0.2	1.05	16	15 ± 2
0.3	1.74	13	12 ± 2
Solutions of 0.012 M $C_{12}EO_6$ + 0.2 M Na_2SO_4			
0.0	0.22	5	12 ± 2
0.05	1.40	6	10 ± 2
0.1	1.44	7	8 ± 1
0.2	1.43	7	9 ± 1

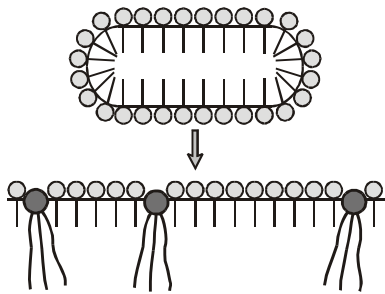
Desorbing micelles: **EO5** – completely full; **EO6**: partially filled

Height of the Kinetic Barrier to Adsorption

For the solutions of C₁₂E₅ we have $\chi \approx k_{1,a} = P \exp(-E_a/kT)$,

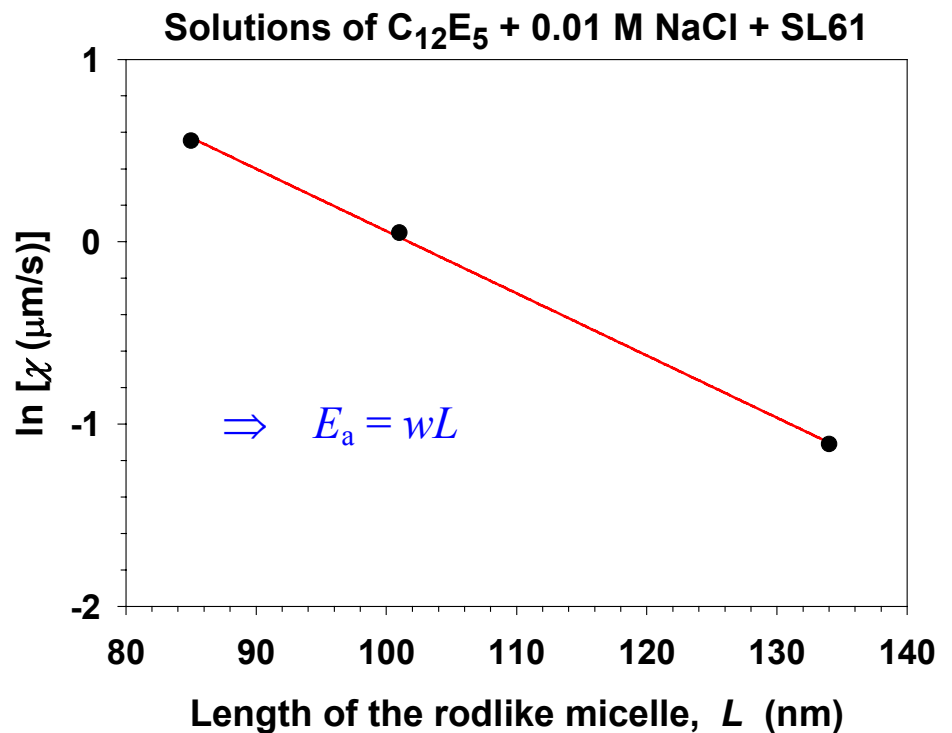
P is a pre-exponential factor and E_a is the activation energy;

L – length of the rodlike micelles; w – activation energy per unit length.



The slope yields:

$$w = 0.034 kT \text{ per nm}$$



For: $L = 50, 100$ and 150 nm

$E_a = 1.7, 3.4$ and $5.1 kT$, respectively.

\Rightarrow The addition of SL61 to the solution of nonionic surfactant decreases the length of the rodlike micelles, thus reducing the kinetic barrier to adsorption and accelerating the solubilization process.

Summary and Conclusions

(A) Solubilization as a **Bulk** Reaction:

- **Water-Soluble Oil** (decane, benzene)
- **Ionic Surfactant (SDS)**

Theoretical model development and comparison with the experiment:

- ⇒ k_+ – **rate constant of solubilization;**
- ⇒ α – **mass transfer coefficient for oil.**

The act of catching of an oil molecule by a micelle occurs under a **barrier** (rather than diffusion) **control**.

(B) Solubilization as a **Surface** Reaction:

- **Water-Insoluble Oil** (triglycerides: triolein, soybean oil)
- **Nonionic Surfactant (C₁₂EO_n + Synperonic L61 + Electrolyte)**

Investigation of the mixed micelles: giant aggregates containing

- **hundreds to thousand surfactant molecules;**
- **dozens of polymer (SL61) molecules**

Theoretical model development and comparison with the experiment

- ⇒ $\chi \approx k_a$ – **compound rate constant of solubilization;**
- ⇒ n_s – **number oil molecules in a swollen micelle;**
- ⇒ **SL61 promotes solubilization by decreasing the barrier to micelles adsorption at the oil-water interface.**

REFERENCES

1. P. D. Todorov, P. A. Kralchevsky, N. D. Denkov, G. Broze, and A. Mehreteab, "**Kinetics of Solubilization of *n*-Decane and Benzene by Micellar Solutions of Sodium Dodecyl Sulfate**", *J. Colloid Interface Sci.* **245** (2002) 371–382.
2. N. C. Christov, N. D. Denkov, P. A. Kralchevsky, G. Broze, and A. Mehreteab, "**Kinetics of Triglyceride Solubilization by Micellar Solutions of Nonionic Surfactant and Triblock Copolymer: 1. The Empty and Swollen Micelles**", *Langmuir* (2002) – in press.
3. P. A. Kralchevsky, N. D. Denkov, P. D. Todorov, G. S. Marinov, G. Broze, and A. Mehreteab, "**Kinetics of Triglyceride Solubilization by Micellar Solutions of Nonionic Surfactant and Triblock Copolymer: 2. Theoretical Model**", *Langmuir* (2002) – in press.
4. P. D. Todorov, G. S. Marinov, P. A. Kralchevsky, N. D. Denkov, P. Durbut, G. Broze, and A. Mehreteab, "**Kinetics of Triglyceride Solubilization by Micellar Solutions of Nonionic Surfactant and Triblock Copolymer: 3. Experiments with Single Drops**", *Langmuir* (2002) – in press.